

Foundation Stage

<u>Key Vocabulary:</u> share, half, equal, unequal, fair, unfair, groups, each.

Objective & Strategy	Concrete	Pictorial	Abstract
To begin to divide by sharing. Children will use a range of concrete resources to share beginning to demonstrate understanding of equal groups.		Children will understand equal groups and share items out in play and problem solving.	
_	Recognise using vocabulary such as 'fair' and 'unfair' groups in	Step 1: Count how many you have.	
	context.	Step 2: Share them equally using 1 to each group at a time, so each group has the same amount.	
		Step 3: Count how many are in each group.	

Symbol Equel sign

35 ÷ 7 = 5

Divisor

Dividend

Symbol Equel sign

Quotient

Year 1

Key Vocabulary: division, dividing, grouping, sharing, doubling, halving, array, number pattern, equal, odd, even, dividend, divisor, quotient.

Objective & Strategy	Concrete	Pictorial	Abstract
To divide by sharing To half a number up to 20.	Children will use concrete resources, including uni-fix cubes to share into equal groups. Children will also be able to half a number up to 20 by sharing into equal groups. Stem Sentence: 12 divided equally between 2 groups equals 6 in each group.	Children will draw jottings and have pictorial representations to demonstrate knowledge of equal groups. 12 ÷ 2 = 6 Iknow there are 2 groups and in each group there are 6 flowers. 12 ÷ 2 = 6 Stem Sentence: equally between 2 groups equals 6 in each group.	Children will be introduced to simple word problems to solve division problems. 12 sweets are shared between 2 people. How many do they have each? 12 ÷ 2 = 6 Stem Sentence: 12 divided equally between 2 groups equals 6 in each group.
To divide by grouping.	Children will begin to solve division problems, which require sorting objects and quantities into 2s, 5s and 10s. Children will use concrete resources such as cubes, counters or objects to aid understanding. 10 cubes are put into groups of 2. How many groups? Stem sentence: 10 cubes are put into groups of 2. There are 5 equal groups.	Children will also experiment dividing by grouping using the bar model. The children will be given a number or picture representatives. This will represent the whole. They then need to split the whole into the number of groups they are dividing by and work out how many would be in each group. 10 cubes are put into groups of 2. How many groups? There are 5 equal groups.	

35 ÷ 7 = 5

Dividend

Quel sign

Quel sign

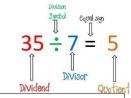
Quel sign

Quel sign

Year 2

Key Vocabulary: division, dividing, grouping, groups of, sharing, doubling, halving, array, number pattern, equal, unequal, odd, even, dividend, divisor, quotient.

Objective & Strategy	Concrete	Pictorial	Abstract
To divide by sharing.	Children will use a range of concrete resources, including cubes to share objects and quantities into equal groups.	Children will use pictures and shapes to share quantities. 12 ÷ 3 =	Children will be writing division number sentence using the divide symbol.
	I have 12 cubes, can you share them equally into 3	4	12 ÷ 3 = 4
	groups?		12 ÷ 4 = 3
			<u>Stem Sentence:</u> 12 divided equally between 3 groups equals 4 in each group.
		Children will also be able to use the bar model to show and support their understanding. e.g. 12 ÷ 4 = 3 12 1000 1000 1000 1000	12 divided equally between 4 groups equals 3 in each group.
	Stem Sentence: 12 divided equally between 3 groups equals 4 in each group.	Stem Sentence: 12 divided equally between 3 groups equals 4 in each group. 12 divided equally between 4 groups equals 3 in each group.	

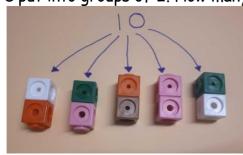


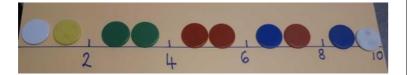
To divide by grouping.

Children will begin to solve division problems, which require sorting objects and quantities into 2s, 5s and 10s.

Children will use concrete resources such as cubes, counters or objects to aid understanding.

10 cubes are put into groups of 2. How many groups?





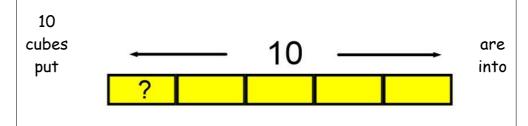
Stem sentence:

 $\underline{10}$ cubes are put into groups of $\underline{2}$. There are $\underline{5}$ equal groups.

Children will also experiment dividing by grouping using the bar model.

The children will be given a number or picture representatives.

This will represent the whole. They then need to split the whole into the number of groups they are dividing by and work out how many would be in each group.



groups of 2. How many groups?

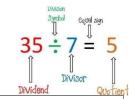
Stem sentence:

<u>10</u> cubes are put into groups of $\underline{2}$. There are $\underline{5}$ equal groups.

Children will use grouping to solve missing number problems

e.g. 10÷ <u>?</u> = 2 Stem Sentence

10 cubes are put into ? equal groups. There are 2 in each group.



To use related multiplication and division facts using the inverse for the 2,5 and 10 times table.

Children will use concrete resources, including cubes to represent arrays. These will then form part of the learning process to explain number related facts and begin to write these in number form.

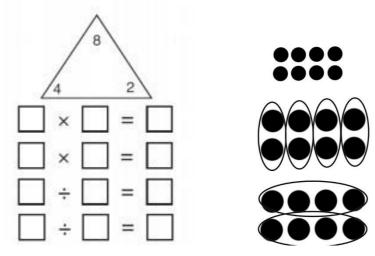
2 x 4 =8

 $4 \times 2 = 8$ $8 \div 2 = 4$

2 = 4 8 ÷ 4 = 2



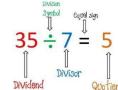
Children will use pictorial representations including arrays to solve missing number facts that demonstrate related facts.



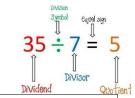
Children will show all 8 related number sentences to demonstrate related facts.

2 x 4 = 8 4 x 2 = 8 8 ÷ 2 = 4 8 ÷ 4 = 2 8 = 2 x 4 8 = 4 x 2 2 = 8 ÷ 4 4 = 8 ÷ 2

Year 3



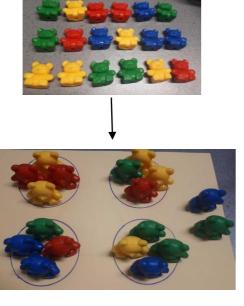
Objective	Concrete	Pictorial	Abstract
To divide 2 digit numbers by partitioning.	Children will use concrete resources, including place value counters and base ten to divide by partitioning	Children will continue to use partitioning representing base 10 pictorially	g the There are 96 footballs. They are shared between 3 teams. How many footballs does each team get?
	96÷3=	96÷3=	96 ÷ 3 = 32
	Step 1: Partition the dividend into tens and ones		How many analysis of 3 in 902 How
	Step 2: share the tens into equal groups as shown by the divisor.		How many groups of 3 in 90? How many groups of 3 in 6? How many groups of 3 in 96?
	(If they do not divide exactly exchange the remaining tens for ones)	Children will also continue to use the bar model to support their understanding.	
		96	
		32 32 32	
	Step 3: share the ones into equal groups as shown by the divisor.		
	Step 4: Add the tens and ones from one group to find the quotient.		
To use arrays to divide.	Children will link division to multiplication by using arrays. They will begin writing numbers sentences to show what they	Children will draw or be given a pic representation of an array. They will circle the	•
	can create.	to split i	t into sentences.
	6 x 4 = 24	multiplicatio	
	4 x 6 = 24 24 ÷ 6 = 4	division sente	6 x 4 = 24
	24 ÷ 4 = 6	24 ÷ 6 = 4	4 × 6 = 24
	00000		24 ÷ 6 = 4 24 ÷ 4 = 6
		STEM: 4 multiplied by 6 equals 24 so 24 divide	ed by 6
		equals 4.	



To divide with whole numbers and represent remainders.

Children will use a range of concrete resources to divide between groups and see what is left over.

 $18 \div 4 = 4 r 2$



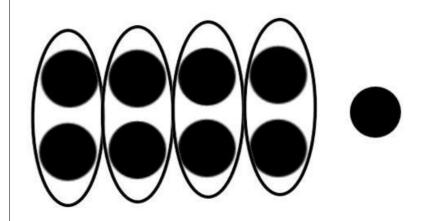
Stem Sentence:

18 divided by 4 equals 4 in each group and 2 left over.

18 divided by 4 must have a remainder because I know that 4x4=16 and 18 is 2 more.

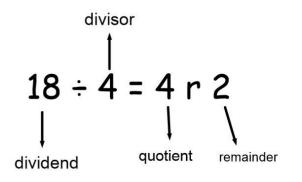
Children will draw equal groups to solve division must be equal and any others are remainders.

9÷4=2r1



9 divided by 4 equals 2 in each group and 1 left over.

Children will complete written division number problems with remainders, understanding that groups sentences using the division symbol and r to represent the remainder.

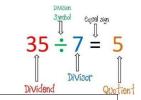


Stem Sentence: 18 divided by 4 equals 4 in each group and 2 left over.

Year 4

Key Vocabulary: factors, multiples, division, dividing, grouping, groups of, sharing, doubling, halving, array, number pattern, equal, unequal, odd, even, dividend, divisor, quotient.

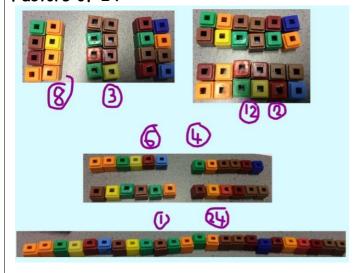
Objective & Strategy	Concrete	Pictorial	Abstract



To recognise and use factor pairs and commutativity in mental calculations.

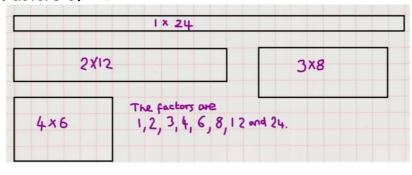
Children use physical objects to create arrays to support their understanding of factors.

Factors of 24



Children investigate finding all factors of a number by drawing arrays.

Factors of 24



Children use their knowledge of multiplication and division facts to find factors of numbers.

Factors of 24

1 × 24 = 24

2 x 12= 24

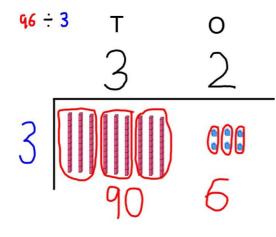
 $3 \times 8 = 24$

 $4 \times 6 = 24$

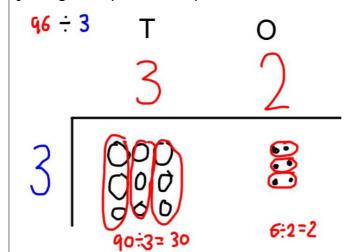
To use a formal written method of short division.

2/3 digit ÷ 1 digit number (exact answers- no remainders) Children represent division calculations using concrete materials such as base 10 and place value counters.

The children partition the dividend and put inside the bus stop then divide each part by the divisor. The quotient is then recorded on the top line.



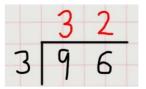
Children represent division calculations using informal jottings and pictorial representations.

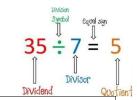


They begin to explore calculations involving simple remainders.

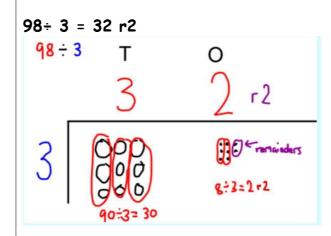
In Year 4 children divide numbers up to 3 digits by a 1 digit numbers with exact answers.

The children are introduced to the bus stop method as a formal written method.





2 or 3 digit divided by a 1 digit number (simple remainders) They begin to explore calculations involving simple remainders.



Once children have a secure understanding, they begin to understand how to record calculations with simple remainders.

Children apply their knowledge of division to word problems.

Arron has 77 seeds. He plants 4 seeds in each plant pot. How many pots does he need?

Year 5

Key Vocabulary: factors, multiples, groups of, share, equal groups, division, divided by, divided into, left over, remainder, array, prime numbers, composite numbers, grouping, groups of, sharing, doubling, halving, array, number pattern, equal, unequal, odd, even, dividend, divisor, quotient.

Objective &	Concrete	Pictorial	Abstract
Strategy			

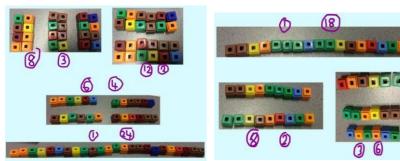


To recognise and

To recognise and use factor pairs of a number and find common factors of two numbers.

Children use physical objects to create arrays to support their understanding of factors.

Find the common factors of 18 and 24



Factors of 24

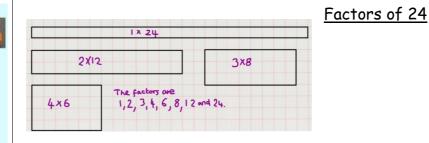
Factors of 18

The common factors are 1, 2, 3 and 6.

Children investigate finding factors by drawing arrays to find all solutions. They then find factors which belong to both numbers.

Factors of 18

Find the common factors of 18 and 24



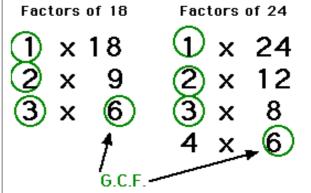
2×9

The factors are
1,2,3,6,9,18

The common factors are 1, 2, 3 and 6.

Children use multiplication and division facts to find factors of numbers.

Find the common factors of 18 and 24



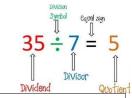
The common factors are 1, 2, 3 and 6.

This three-digit number has 2 and 7 as factors.

2 9 4

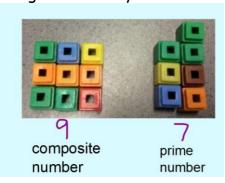
Write another three-digit number which has 2 and 7 as factors.



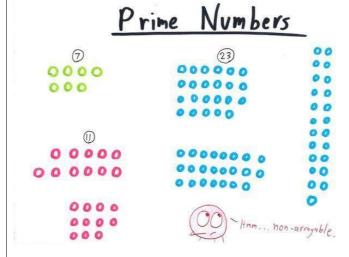


To establish whether a number up to 100 is prime and recall prime numbers up to 19.

Children find prime numbers and composite (non-prime numbers) by using arrays. They understand that composite numbers form arrays and prime numbers cannot be arranged into arrays.

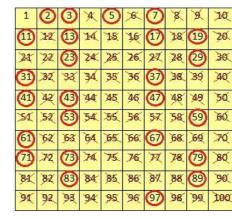


Children use jottings and pictorial representations to investigate composite and prime numbers.

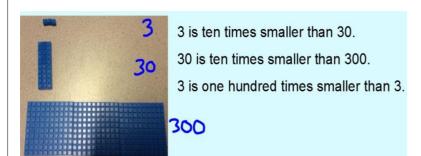


Children use their knowledge of multiples and factors to find the prime numbers up to 100. They eliminate numbers that have factors other than 1. They can recall

all prime numbers up to 19.



To divide whole numbers and those involving decimals by 10, 100 and 1,000 Children use resources to understand what 10, 100 and 1000 times bigger looks like.

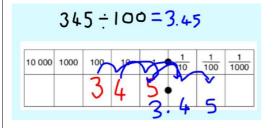


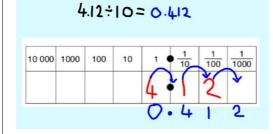
Children use place value grids to divide numbers by 10, 100 and 1000s. They understand the movement of the digits on the place value

grid.



Dividing





They apply this knowledge to decimal numbers.

Children apply their knowledge of place value to divide numbers by 10, 100 and 1000, including decimal numbers.

3450÷ 10 = 345 345÷100= 3.45 2.67 ÷10= 0.267 12.7÷1000= 0.0127

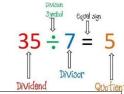
They apply their understanding to more complex number puzzles and word problems.

Circle the number that is 10 times greater than nine hundred and seven.

9,700 907 9,007 970 9,070

Write the missing number to make this division correct.

A PS4 is on for sale at a tenth of its original price. It usually costs£450.90. How much is it at the sales?

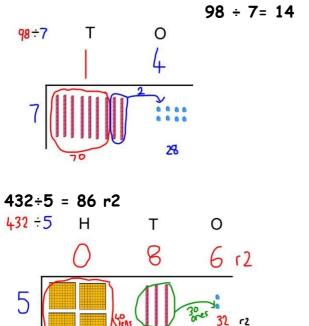


To use a formal written method of short division.

Numbers up to 4 digits ÷ 1 digit number (with remainders)

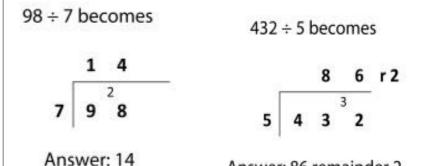
Children represent division calculations using concrete materials such as base 10 and place value counters.

The children partition the dividend and put inside the bus stop then divide each part by the divisor. The quotient is then recorded on the top line. The children work with numbers that involve remainders.



Children represent division calculations using informal jottings and pictorial representations. The children recognise remainders.

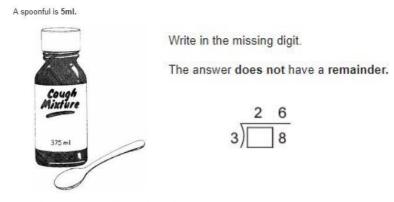
In Year 5 children divide numbers up to 4 digits by a 1 digit number, including calculations involving remainders. The children continue to use the bus stop method as a formal method of written calculation.



Children are expected to interpret non-integar answers by expressing results as fractions (432÷5 = 86 $\frac{2}{5}$), decimals (432÷5 = 86.4) or by rounding (432÷5 = 86.4 \approx 86 sweets) according to the context.

Answer: 86 remainder 2

Children apply their knowledge using word problems and number puzzles.



How many spoonfuls can you get from this bottle?

Symbol cavel sign

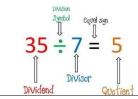
35 ÷ 7 = 5

Dividend Quotien

Year 6

<u>Key Vocabulary:</u> factors, multiples, groups of, share, equal groups, division, divided by, divided into, left over, remainder, array, prime numbers, composite numbers, grouping, groups of, sharing, doubling, halving, array, number pattern, equal, unequal, odd, even, dividend, divisor, quotient.

Objective & Strategy	Concrete	Pictorial	Abstract
To identify common factors.	Children use physical objects to create arrays to support their understanding of factors. Find the common factors of 18 and 24 Factors of 24 Factors of 18 O O O O O O O O O O O O O	Children investigate finding all factors of a number by drawing arrays. They then find factors which are the same in both numbers. Find the common factors of 18 and 24 Factors of 24 The factors ove 1,2,3,4,6,8,12 and 24.	·
	The common factors are 1, 2, 3 and 6.	Factors of 18 2x9 The factors are 1,2,3,6,9,18 The common factors are 1, 2, 3 and 6.	The common factors are 1, 2, 3 and 6.
To establish whether a number up to 100 is prime and recall prime numbers up to 19.	Children find prime numbers and composite (non-prime numbers) by using arrays. They understand that composite numbers form arrays and prime numbers cannot be arranged into arrays. Prime number	Children use jottings and pictorial representations to Prime Numbers 23 23 24 25 26 27 28 29 29 29 20 20 20 20 20 20 20	Children use their knowledge of multiples and factors to find the prime numbers up to 100. They eliminate numbers that have factors other than 1. They can recall all prime numbers up to 19.

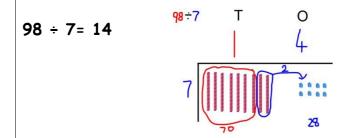


To use a formal written method of short division.

Larger numbers ÷ 1 digit number (involving remainders)

Children represent division calculations using concrete materials such as base 10 and place value counters.

The children partition the dividend and put inside the bus stop then divide each part by the divisor. The quotient is then recorded on the top line. The children work with numbers that involve remainders.



jottings and pictorial representations. The children will recognise remainders.

Answer: 86 remainder 2

Children represent division calculations using informal In Year 6 children divide larger numbers by a 1 digit number with calculations involving remainders. The children continue to use short division method as a formal method of written

calculation. 98 ÷ 7 becomes 432 ÷ 5 becomes 1 4 8 6 r2 7 9 8 4 3 2

Children are expected to interpret non-integar answers by expressing results as fractions $(432 \div 5 = 86)$, decimals $(432 \div 5 = 86.4)$ or by rounding $(432 \div 5 =$ $86.4 \approx 86$ sweets) according to the context.

Answer: 86 remainder 2

Children apply their knowledge using word problems and number puzzles.

Sharon buys a pack of 24 cans of lemonade for £6. How much does each can cost?

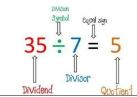
Write the missing number.

Answer: 14

70 ÷ = 3.5

Write the missing number in each calculation

= 3 remainder 4 25

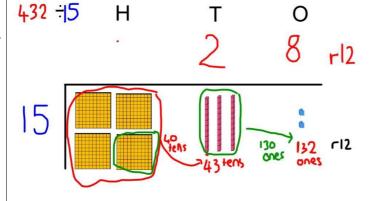


To use a formal written method of long division.

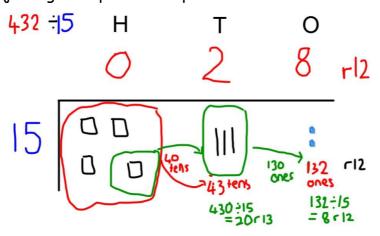
Divide larger numbers ÷ 2 digit numbers (involving remainders)

Children represent division calculations using concrete materials such as base 10 and place value counters.

The children partition the dividend and put inside the bus stop then divide each part by the divisor. The quotient is then recorded on the top line.



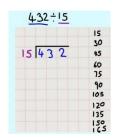
jottings and pictorial representations.



Children represent division calculations using informal | The children use short division method as a formal method of written calculation. They use their understanding of the pictorial and concrete stages to understand the value of each number.

$$432 \div 15 = 28^{\frac{12}{15}}$$

Step one: Children will put the calculation into the grid and list their multiples of the divisor.



Step 2: Use the multiples list and jottings to divide each digit the same as short division, carrying remainders to the next place.

Step 3: The number left is your remainder; record this as a remainder fraction (or decimal to two decimal places) 432 ÷ 15 = 28 r 12/15 or 28.75

Children are expected to interpret non-integar answers by expressing results as fractions (432÷15 = $28^{\frac{12}{15}}$ = $28^{\frac{4}{5}}$ decimals (432÷15 = 28.8) or by rounding (432÷15 = 28.8 \approx 29 cars) according to the context.